

# Methodology for renewable power generation and optimization of hybrid solar / wind power system using IEEE load pattern

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**Abstract-** The most important application field of this search is renewable energy resources. Wind and solar energy have been popular ones owing to abundant, ease of availability and convertibility to the electric energy. Initially the elements of solar and wind turbine is studied and the main component of both systems is identified. Long term data of Wind Speed and irradiance level were considered for IEEE load pattern for a year. For a considered load and desired loss of power supply probability, an optimum number of batteries and PV modules were computed based on the minimum cost of the system using MATLAB R2007a (Version 7.4) software. The mathematical model for characterizing PV module and Wind generator was developed. Graphical optimization for the number of battery and PV module has been carried out to minimize the cost of system for desired loss of power supply probability.

**Key words:** Hybrid system, PV module, Optimization, Loss of power supply probability.

## I. INTRODUCTION

The development of wind power in India began in the 1990s, and has significantly increased in the last few years. It is estimated that 6,000 MW of additional wind power capacity will be installed in India by 2012. Wind power accounts for 6% of India's total installed power capacity, and it generates 1.6% of the country's power. The daily average solar energy incident over India varies from 4 to 7 kWh/m<sup>2</sup> with about 1500–2000 sunshine hours per year (depending upon location), which is far more than current total energy consumption. By complimenting the properties of solar and wind energy sources for certain locations, a Hybrid PV/Wind system with storage banks presents an unbeatable option for the supply of small electrical loads at remote locations where there is no utility grid power supply.

Methodology for optimal sizing the wind /PV hybrid system was given by Borowy and Salmeh [1] that calculates the optimum size of a battery bank and the PV array for a hybrid system based on the minimum cost of the system using graphical construction technique. Based on Genetic algorithm technique optimum match design sizing method for hybrid solar wind system was developed by Hongxing *et.al* [2]. Diaf *et.al* [3] presented a mathematical models for characterizing PV module, wind generator and battery considering various types and capacities of system devices and the configuration that meet the desired system reliability by changing the type and size of the devices system. Wang and Singh [4] presented the optimal design of an autonomous hybrid generating system including different power sources such as wind turbine generator, photovoltaic and storage batteries. A constrained mixed-integer multi objective particle swarm optimization (CMIMOPSO) algorithm was adopted to derive non dominated solutions for the optimal design. Due to its simple operations and good convergence performance, PSO has turned out to be outstanding heuristics for numerous complex engineering design problems and also an optimization procedure was developed to simultaneously minimize the system cost as well as maximize the system reliability. A probabilistic approach based on the convolution technique to assess the long term performance of a hybrid for both standalone and grid-linked applications was provided by Tina *et.al*. [5]. This approach uses energy index of reliability (EIR) directly related to energy expected to estimate energy performance of HSWPS for the reliability analysis. Yang and Burnett [6] used simulation model for analyzing the probability of power supply failure in hybrid photovoltaic wind power generation systems incorporating a storage battery bank and also analyzes the reliability of the systems, for the loss of power supply probability (LPSP) analysis.

The objective functions were number of battery and number of PV module. 8736 irradiance level and wind speed data for a year was used for optimal design model of hybrid system. Wind turbine and PV power output were matched to a given load demand that was a load of a year. For every hour of a typical day in each month, power output of both a wind turbine and a PV module were calculated. Then for a given loss of Power Supply Probability, the combinations of a number of PV modules and a number of batteries were also calculated. The choice of the optimum number of PV modules and batteries was based on the minimum cost of the system using graphical optimization techniques of Rao [7].

## II. NOMENCLATURE

$A$	Current change temperature coefficient at reference insolation (Amps/ $^{\circ}$ C)
$\beta$	Voltage change temperature coefficient at reference insolation (Volts/ $^{\circ}$ C)
$I$	Module Current (Amps)
$I_{mp}$	Module Max Power Current (Amps)
$I_{sc}$	Module Short Circuit Current (Amps)
$S$	Total Tilt Insolation (W/sq.m)
$S_{ref}$	Reference Insolation (W/sq.m)
$R_s$	Module Series Resistance (Ohms)
$T$	Cell Temperature ( $^{\circ}$ C)
$T_A$	Ambient Temperature ( $^{\circ}$ C)
$T_{ref}$	Reference Temperature ( $^{\circ}$ C)
$\Delta T$	Change in Cell Temperature ( $^{\circ}$ C)
$V$	Module Voltage (Volts)
$V_{mp}$	Module Max Power Voltage (Volts)
$V_{oc}$	Module Open Circuit Voltage (Volts)
$P_{pv}$	Power generated due to PV module (KW)
$V$	Wind speed at projected height, H (m/s)
$V_i$	Wind speed at reference height, $H_i$ (m/s)
$\alpha$	1/7, Power law exponent
$P_r$	Rated electrical power (KW)
$V_c$	cut in wind speed (m/s)
$V_r$	rated wind speed (m/s)
$V_f$	cut off wind speed (m/s)
$P_w$	power generated by Wind turbine (KW)
$E_{B(t)}$	energy stored in batteries at any time t
$E_{Bmin}$	battery minimum allowable energy
$\eta_{in}$	efficiency of the inverter
$\eta_{batt,in}$	round-trip efficiency of the batteries
$E_B(t)$	energy stored in batteries in hour t(KW)
$E_B(t-1)$	energy stored in in previous hour(KW)
$E_L(t)$	load demand in hour t. (KW)
$E_w(t)$	energy generated by wind turbine(KW),
$E_{PV}(t)$	energy generated by a PV module KW)
$NPV$	number of PV modules in a PV Array
$LPSP$	loss of power supply probability
$LPS(t)$	loss of power supply at hour t.
$T$	period of time

## III. RENEWABLE POWER GENERATION METHODOLOGIES

### A. calculation of the PV module average power output.

Solar array modules are arranged so that there are sufficient series connected solar cells to generate enough voltage to charge a battery. Modules are arranged in series to increase the system voltages and in parallel to increase the

system output current. The power output of the PV module P(s) is a product of the module output voltage and output current.

The module equivalent circuit output current 'I' can be expressed as a function of the module output voltage V.

$$I(V) = I_{sc} \left\{ 1 - C_1 \left[ \exp\left(\frac{V + \Delta V}{C_2 V_{oc}}\right) - 1 \right] \right\} + \Delta I \tag{1}$$

where:

$$C_2 = \frac{V_{mp}/V_{oc} - 1}{\ln(1 - I_{mp}/I_{sc})}$$

$$C_1 = (1 - I_{mp}/I_{sc}) \cdot \exp[-V_{mp}/(C_2 \cdot V_{oc})]$$

$$\Delta I = \alpha(S/S_{ref}) \Delta T + (S/S_{ref} - 1) \cdot I_{sc}$$

$$\Delta V = -\beta \cdot \Delta T - R_s \cdot \Delta I$$

$$\Delta T = T - T_{ref}$$

$$T = T_A + 0.02 \cdot S$$

Then module output voltage and Power generated are calculated using the formulas given below.

$$P_{pv} = V \cdot I - I^2 R_s$$

MATLAB R2007a program is used for the calculation of solar power and the Graph is plotted between the solar power and the solar radiation as shown in fig 2.

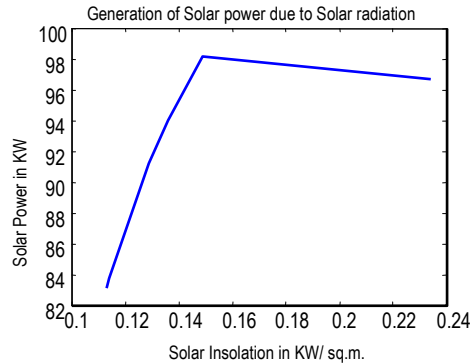


Fig 1.Generation of solar power due to solar radiation

**B. Calculation of available Wind generator power**

Wind energy is ample, renewable, widely distributed, clean, and works against the greenhouse effect if used to replace the use of fossil-fuel.. The wind speed data were recorded near the ground surface. It should be converted to hub height using the required formula. The formula used for the calculation of wind speed is given as below

$$V = V_i (H/H_i)^\alpha \tag{2}$$

Calculation of available Wind generator power is performed with the help of following formulas. The available wind generator power output is a function of the wind velocity. This wind power is calculated for each hour of a typical day in every month.

$$P_w = Pr (V - V_c) / (V_r - V_c) \text{ for } (V_c \leq V \leq V_r) \tag{3}$$

$$P_w = Pr \text{ for } (V_r \leq V \leq V_f)$$

$P_w = 0$  otherwise

### C. Model Used for Solar/ Wind Hybrid System.

The initial cost of the renewable generation facilities is quite expensive and there is also maintenance cost. Thus it is desirable to make use of renewable in an appropriate fashion in order to achieve a cost effective and reliable autonomous hybrid power generation system (Fig 2). A suitable combination of these power sources is able to reduce the generation costs as well as enhance the overall system reliability.

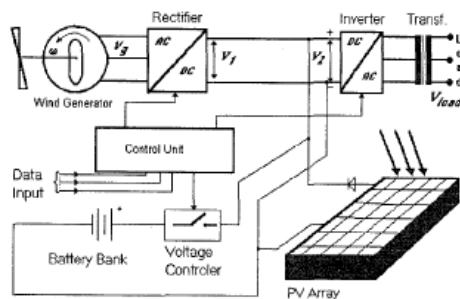


Fig. 2. Wind/PV Hybrid system

### D. loss of power supply probability (LPSP)

Loss of Power Supply Probability can be defined as the long-term average fraction of the load that is not supplied by a stand-alone system. Energy is stored in batteries when the generated power by the wind turbine and PV array is greater than the load. When the power generated is less than the load, the energy is taken from the batteries. The state of charge of the batteries was used as a decision variable for the control of the overcharge and discharge. The case of overcharge may occur when high power is generated by the photovoltaic and wind turbine, or when low load demand exists. In such a case when the state of charge of the batteries reaches the maximum value  $B_{max}$  the control system intervenes and stops the charging process.

On the other hand, if the state of charge decreases to a minimum level  $B_{min}$  the control system disconnects the load. This is important to prevent batteries against shortening their life or even their destruction. In terms of state of charge of batteries, the loss of Power Supply Probability can be therefore defined as:

$$LPSP = \Pr \{ E_{B(t)} \leq E_{Bmin}; \text{ for } t \leq T \} \quad (4)$$

i.e. the probability of the state of charge at any accumulative time  $t$ , within the time period  $T$ , to be less or equal than the minimum level  $E_{Bmin}$ .

## IV. SIMULATION MODEL

The performance of batteries is complicated and cannot be precisely predicted for uncontrolled charge/discharge cycles in stand-alone systems. Moreover, the battery capacity is defined in terms of the amount of energy that can be extracted, not the amount that is actually stored. Therefore, the battery charge efficiency was set equal to the round-trip efficiency, and the discharge efficiency was set equal to 1. The inverter is rated in terms of the peak load demand. The efficiency of the inverter is a function of the ratio of actual load to the inverter's rating. In this paper, we used a constant value of inverter efficiency based on the average load demand.

### A. Derivation of the Simulation Model

The energy generated by wind turbine and PV array for hour  $t$ ,  $EG(t)$  can be expressed as follows:

$$EG(t) = E_w(t) + NPV \times EPV(t) \quad (5)$$

Since we assumed that the battery charge efficiency is set equal to the round-trip efficiency and the discharge efficiency is set equal to 1, we considered two cases in expressing current energy stored in the batteries for hour t. If the generated energy from the wind turbine and PV array exceeds that of the load demand, the batteries will be charged with the round-trip efficiency.

$$EB(t) = EB(t-1) + (EG(t) - EL(t) / \eta_{in}) \cdot \eta_{batt, in} \quad (6)$$

When the load demand is greater than the available energy generated, the batteries will be discharged by the amount that is needed to cover the deficit. It can be expressed as follows:

$$EB(t) = EB(t-1) - \{ EL(t) / \eta_{in} - EG(t) \} \quad (7)$$

### B. Constraints

The energy stored in batteries at any hour t is subject to the following constraint:

$$EB_{min} \leq EB(t) \leq EB_{max} \quad (8)$$

The generated power is subjected to following constraint

$$EG(t) > EL.$$

When the available energy generated and stored in batteries is insufficient to satisfy the load demand for hour t, that deficit is called as Loss of Power Supply for hour t and can be expressed as:

$$LPS(t) = EL(t) - \{ EG(t) + EB(t-1) - EB_{min} \} \eta_{inv} \quad (9)$$

The Loss of Power Supply Probability for a considered period of time T is the ratio of all LPS (t) values for that period to the sum of the load demand. This can be defined as-

$$LPSP = \sum LPS(t) / \sum EL(t) \quad (\text{for } 1 \leq t \leq T) \quad (10)$$

Once the available energy generated from both a wind turbine and a PV module was determined in the previous steps for every hour of a typical day in each month, different combinations of the number of PV modules and the number of batteries could be calculated for a desired LPSP.

### C. optimization technique used

Graphical optimization is performed for the calculation of optimum number of PV modules and batteries for different values of loss of power supply probabilities. The costing is performed for different number of batteries and PV modules. Then graphs are plotted taking number of batteries on x axis and LPSP, cost on Y axis. The same procedure is done for number of PV modules. Variation of LPSP is observed for different values of PV modules. Then graph is plotted taking number of PV modules on X axis and Cost and LPSP on Y axis. Optimized values are obtained at the intersection of the graphs. The optimal point will give the optimized design number of objective variables.

## V. RESULTS AND DISCUSSIONS

### A. Optimization of the hybrid system for one year data

The developed method is used to calculate the optimum number of batteries and PV modules for a stand alone wind/PV system. First the program for the calculation of loss of power supply probability is produced using MATLAB 2007a (Version 7.4 software language). Various combinations of battery with number of PV modules are examined for loss of power supply probability. The cost analysis is done for particular number of batteries and PV modules. Graph is plotted using MATLAB to relate number of objectives (PV module number, battery number) with the cost and corresponding LPSP. Battery capacity is taken as 50 Ah and the cost of battery is 1500 \$.

The specifications used for the PV module considered in the program are as given below.

Table 1. Specifications of PV module

Vsc (v)	Isc (A)	Vmax (v)	Imax (A)	Pmax (W)	Cost (\$)
21	6.5	17	5.73	100	6500

The specifications used for Wind turbine are as follows

Table 2. Specifications of the Wind turbine.

Pr (KW)	vc (m/s)	Vr (m/s)	vf (m/s)	H(m)	Hi (m)
6	2.5	10	25	20	8

*B. Solar and Wind speed Data used for IEEE hourly load pattern*

Fig 3 & 4 shows meterological parameters i.e. 8736 solar irradiation level and Wind speed data, Mani [8, 9], of an year for IEEE hourly load pattern

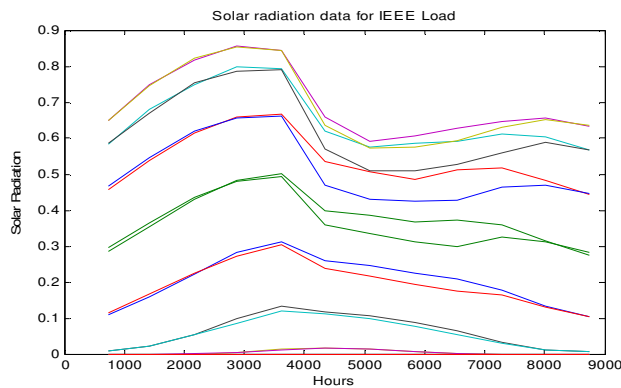


Fig 3. Solar radiation data for IEEE hourly load system

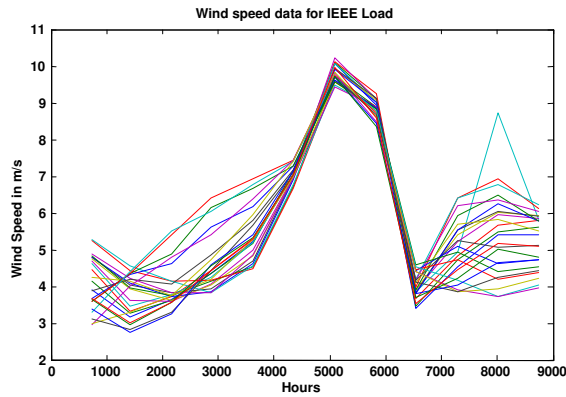


Fig 4. Wind speed data for IEEE hourly load system

*C. Optimization of battery number for IEEE hourly load pattern*

By using optimization methodology the optimum number of battery and PV module are computed for IEEE hourly load pattern. The results of optimal sizing are given in Table 3. In the Fig. 5, the optimal design number for battery is coming as 4 and corresponding optimized cost of 4 batteries will be \$ 6000.

Table 3. Optimal sizing results for number of batteries for IEEE load

Npv	Nbat	Cbat (Ah)	LPSP	Price (1500 US \$ / KW / battery)
10	2	100	0.7025	3000
10	3	100	0.6867	4500
10	4	100	0.6709	6000
10	6	100	0.6393	9000
10	8	100	0.6077	12000
10	10	100	0.5762	15000
10	12	100	0.5446	18000

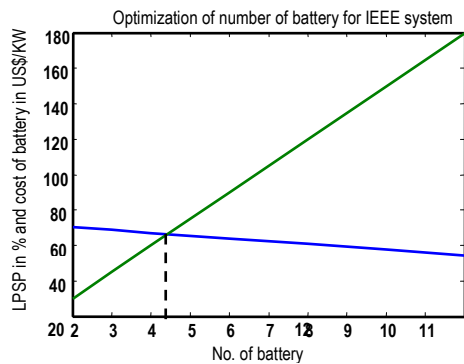


Fig 5. Optimization of battery number for IEEE hourly load system

#### D. Optimization of number of PV module for IEEE hourly load pattern system.

The results obtained are given in Table 4. As seen from Fig.6, the optimal design number for PV module is coming as 10 and the optimized cost of 10 PV modules will be 65000 \$.

Table 4. Optimal sizing results for number PV modules for IEEE load

Npv	Nbat	Cbat (Ah)	LPSP	Price 6500 US \$ /KW /PV module)
6	5	100	0.6836	39000
8	5	100	0.6694	52000
10	5	100	0.6551	65000
12	5	100	0.6409	78000
14	5	100	0.6266	91000

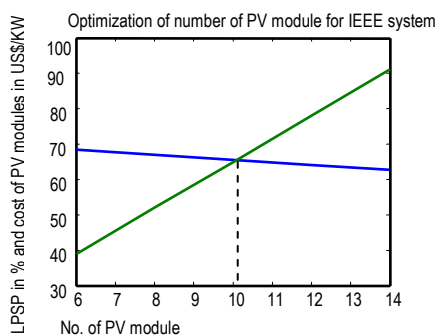


Fig 6. Optimization of PV module number for IEEE hourly load system.

## VI. CONCLUSION

A methodology for calculation of the optimum size of a battery bank and the optimum size of a PV array in a hybrid wind/PV system for a given load is interesting because it allows to study technico-economic aspects of a hybrid system with two renewable system (Wind generator and Solar module) and electrochemical storage system (battery bank). It is based on the use of long term data for both wind speed and irradiance levels. The power outputs of both the wind turbine and the PV module were calculated. For a given Loss of Power Supply Probability, a different combination of the number of PV modules and the number of batteries was calculated. An optimum design choice depends on the relative costs of a PV module and a battery. We assumed that total cost of the system is linearly related to both the number of PV modules and the number of batteries. The minimum cost will be at the point at which cost line and the LPSP line are intersecting. The optimal design value for number of battery is 4 which costs 6000\$ for and IEEE load pattern. The optimal design number for PV module in IEEE system is 10 with optimized cost 65000 \$. By increasing the number of objective variables i.e. battery number, PV module number decreases loss of power supply probability and improves the reliability of the Hybrid system. With the help of optimization technique we have been able to reduce the cost of hybrid system. The optimum mix of PV modules and batteries depends on the particular site, load profile, and the desired reliability of the hybrid system. The results obtained depend upon the quality of the simulation model and the representivity of the data.



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