SMC based Localization Algorithm for Wireless Sensor Networks

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Abstract – Localization in mobile sensor networks is more challenging than in static sensor networks because mobility increases the uncertainty of nodes positions. The localization algorithms used in the Wireless sensor networks (WSN) are mainly based on Sequential Monte Carlo (SMC) method. The existing SMC based localization algorithms commonly rely on increasing beacon density in order to improve localization accuracy and suffers from low sampling efficiency and also sampling in those algorithms are static and have high energy consumption. Those algorithms cannot able to localize sensor nodes in some circumstances. The main reason for that is in some time slots the sensor node cannot hear any beacon node. This results in localization failure. The Improved Monte Carlo Localization (IMCL) algorithm achieves high sampling efficiency, high localization accuracy even in the case when there is a low beacon density. This can be achieved using bounding box and weight computation techniques. This algorithm also uses time series forecasting and dynamic sampling method for solving the problem of localization failure. Simulation results showed that the proposed method has a better performance in sparse networks in comparison with previous existing method.

Keywords – Mobile Sensor Networks, Localization, Sequential Monte Carlo methods.

I. INTRODUCTION

Wireless sensor networks (WSNs) have been used in many fields, including environmental and habitat monitoring, precision agriculture, animal tracking, and disaster rescue. In many applications, it is essential for nodes to know their positions. For example, data should be labelled with the positions where they are collected to help the scientists perform corresponding analysis. Position information of nodes are also necessary in many network protocols, e.g., clustering and routing which depend on the geographical information of nodes. The procedure through which the nodes obtain their positions is called localization. In localization, the nodes in a sensor network can be categorized into two types: beacon nodes which are aware of their positions and sensor nodes which need to determine their positions using a localization algorithm.

A straightforward method for localization in WSNs is to use existing localization techniques, e.g., attaching a Global Positioning System (GPS) receiver on every sensor node. However, as the scale of sensor networks becomes larger and larger, these methods become infeasible because of their high cost or inconvenience. In some recently emerging applications such as animal monitoring and tracking sensor nodes may move after deployment. These nodes form mobile sensor networks in contrast to traditional static sensor networks in which sensor nodes remain stationary after deployment. The motion of sensor nodes makes most existing localization algorithms designed for static sensor networks inapplicable to mobile sensor networks. There are some localization algorithms specially designed for mobile sensor networks. All of them are based on the Sequential Monte Carlo (SMC) method. This is because the SMC method provides simple simulation-based approaches in estimating the location. Previous SMC-based localization algorithms either suffer from low sampling efficiency or require high beacon density to achieve high localization accuracy. The major problem of most existing SMC-based localization algorithms is that they only rely on increasing beacon density to improve localization accuracy. However, beacon nodes are usually more expensive than sensor nodes. Because there are much more sensor nodes than beacon nodes in a sensor network, it will be very beneficial if sensor nodes can be used to improve the localization accuracy.

In this paper, we propose an efficient algorithm which addresses both aforementioned issues. The algorithm is based on the sequential Monte Carlo Localization (MCL) algorithm named as Improved MCL (WMCL). IMCL
achieves high sampling efficiency and achieves high localization accuracy even when the beacon density is low using bounding box technique and weight computation methods. Despite the above technique having good localization accuracy, sampling in these techniques are static and they have high energy consumption. Also the existing algorithms are not able to localize sensor nodes in some circumstances. The main reason is that in some time slots the node cannot hear any seed node. The Improved Monte Carlo Localization (IMCL) algorithm uses forecasting and dynamic sampling method for localization. This method has the ability of nodes localization in those conditions and it is an energy efficient method.

The paper is organized as follows. The Section 2 deals with related work in localization of Wireless Sensor Networks. Section 3 deals with the proposed Improved Monte Carlo Localization (IMCL) algorithm. Section 4 is devoted to extensive performance analysis. Section 5 deals with the Conclusion and future directions.

II. RELATED WORK

Extensive research has been done on localization for wireless networks. A general survey is done focusing only on localization techniques suitable for ad hoc sensor networks. The approaches taken to achieve localization in sensor networks differ in their assumptions about the network deployment and the hardware’s capabilities.

Centralized localization techniques depend on sensor nodes transmitting data to a central location, where computation is performed to determine the location of each node. Doherty, Pister and Ghaoui developed a centralized technique using convex optimization to estimate positions based only on connectivity constraints given some nodes with known positions. MDS-MAP technique improves on these results by using a multidimensional scaling approach, but still requires centralized computation. Requiring central computation would be infeasible for mobile applications because of the high communication costs and inherent delay, hence we focus on distributed localization techniques.

Distributed localization methods do not require centralized computation, and rely on each node determining its location with only limited communication with nearby nodes. These methods can be classified as range-based and range-free. Range-based techniques use distance estimates or angle estimates in location calculations, while a range-free solution depends only on the contents of received messages. Range-based approaches have exploited time of arrival, received signal strength, time difference of arrival of two different signals (TDOA), and angle of arrival (AOA). Though they can reach fine resolution, either the required hardware is expensive (ultrasound device for TDOA, antenna arrays for AOA) or the results depend on other unrealistic assumptions about signal propagation (for example, the actual received signal strengths of radio signals can vary when the surrounding environment changes). Because of the hardware limitations of sensor devices, range-free localization algorithms are a cost effective alternative to more expensive range-based approaches.

Monte Carlo localization (MCL) method is developed for use in robotics localization for use in mobile sensor network applications. MCL is a particle filter combined with probabilistic models of robot perception and motion. It outperforms other proposed localization algorithms in both accuracy and computational efficiency. The key idea of MCL is to represent the posterior distribution of possible locations using a set of weighted samples. Each step is divided into a prediction phase and an update phase. In the prediction phase, the robot makes a movement and the uncertainty of its position increases. In the update phase, new measurements (such as observations of new landmarks) are incorporated to filter and update data. The process repeats and the robot continually updates its predicted location.

However, there are substantial differences between robot localization and node localization for sensor networks. While robot localization locates a robot in a predefined map, localization in sensor networks works in a free space or unmapped terrain. Second, a robot has relatively good control and probabilistic knowledge of its movement in a predefined map. A sensor node typically has little or no control of its mobility, and is unaware of its speed and direction. Third, a robot can obtain precise ranging information from landmarks, but a sensor node can only learn that it is within radio range. Finally, in robot localization, the individual measurements are integrated multiplicatively, assuming conditional independence between them, and the weights of samples need to be normalized after updating. In MCL, due to the constraints in computing and memory power, a filtering approach is adopted in which each measurement can be considered independently, and the weight of each sample is either 0 or 1.

There are some other variants of MCL, for example, the dual and Mixture MCL, Multihop-based Monte Carlo Localization (MMCL), and Range-based MCL. The dual and Mixture MCL improves the localization accuracy of MCL by exchanging the probability functions used in the sampling step and in the filtering step. It incurs higher computational cost than MCL. MMCL and Range-based MCL use multihop sensor-beacon distances to improve the localization accuracy and to reduce the number of needed beacons. Compared with them, Our WMCL algorithm doesn’t use multihop sensor-beacon distances so incurs much less communication cost and it uses weight computation methods to minimize localization error.
The previous existing methods have two major weak points which are not focused. The first problem is using of constant number of samples for localization. Second is that all nodes in all time slots cannot be localized. The proposed methods will overcome those drawbacks and the methods are discussed below.

III. THE PROPOSED IMCL ALGORITHM

A. Introduction
In IMCL algorithm, the network model is introduced and then the five main parts of IMCL are described as follows: Bounding-box construction, Dynamic sampling, Time series forecasting, Samples weights computing, maximum possible localization error computing.

B. Building the Bounding Box
There are two areas involved in bounding box of IMCL: the candidate samples area and the valid samples area. The candidate samples area is used to draw new candidate samples and the valid samples area is used to filter out invalid samples. When the candidate samples area is large and the valid samples area is small, candidate samples drawn in the sampling step have high probability to be filtered out in the filtering step. Figure 1 shows the construction of bounding box in IMCL algorithm.

In IMCL, the possible locations of a sensor node after move lie in a disk with radius $r_{max}$. So the size of the candidate samples area will increase when $r_{max}$ increases. On the other hand, when $sd$ increases, the size of the valid samples area will decrease. Denote by $V_t$ the total number of candidate samples drawn in the sampling step in time unit $t$ and define the sampling efficiency in $t$ as,

$$e_t = \frac{|S|}{|P_t|}$$

then in WMCL the sampling efficiency will decrease when $r_{max}$ or $sd$ increases, which will cause high computational cost accordingly. Two-Hop beacon neighbours are also used to reduce the size of the bounding-box by replacing $r$ with $2r$. The candidate samples are chosen from the bounding box.

B. Dynamic sampling method
As previously mentioned, instead of taking a fixed number of samples like 50 for localization, we can determine this number dynamically based on the size of the sampling area. It is clear that for a large anchor box, a large number of samples are needed to estimate nodes location accurately. While in the case of small anchor box, we will focus on a small area. For a small area, small number of samples is needed to accurately estimate nodes position.

If created anchor box have the coordinates of $(X_{min}, Y_{min})$ and $(X_{max}, Y_{max})$, so area size of this box is determined and we will specify the number of samples based on this area size. Noting to the standard number of samples that is 50, this number will be used for an anchor box with maximum area size. An anchor box is maximized when the node hears only a one-hop anchor node. In this case the box size will be equal to a square of size $2V_{max}$. So we will consider 50 samples for this box and use equation (5) for other box sizes.
Sample Number = 50*((x_{max} - x_{min}) (y_{max} - y_{min}))/4V_{max}^2 \hspace{1cm} (2)

When the anchor box has the maximum area, numerator and denominator of the fraction in the equation (2) will be equal and so the number of samples will be equal to 50.

For the cases when the anchor box size is more than $4V_{max}^2$, we consider the number of samples equal to 50. Example of such cases is when the sensor node hears only one two-hop anchor node.

C. Linear prediction using time series

Linear prediction method is a powerful technique for predicting time series in a time-varying environment. This method is expressed in equation (6) and is a recursive method

$$y(t + T) = a_1 y(t) + a_1 y(t-T) + ... + a_m y(t-(m-1)T) \hspace{1cm} (3)$$

Estimated value at time t as a linear function of previous values in the times "t-T, t-2T, .. t-mT" has been produced is obtained. In equation(3) $a_1, a_2, ..., a_m$ are the linear prediction coefficients, 'm' is the model degree, 'T' is the sampling time, $y(t+T)$ is the next observation estimation and $y(t), y(t-T), ... y(t-mT)$ are the present and past observations. The prediction error which is the difference between the predicted and the real locations (Equation (4)) must be minimized.

$$\text{Error(\%)} = \frac{\text{Predicted Location} - \text{Real Location}}{\text{Real Location}} \times 100\% \hspace{1cm} (4)$$

In order to estimate the coefficients of linear prediction model we use the least squares error method and rewrite equation (3) with considering modelling error in equation (4):

$$y(t) = a_1 y(t) + a_1 y(t-T) + ... + a_m y(t-(m-1)T) + e(t) \hspace{1cm} (5)$$

The error $e(t)$ is generated because of not adopting the linear prediction model to the real value. So to find the coefficients, $a_1, a_2, ..., a_m$ in equation(5), we use the sum least squares error and set of linear functions presented in equation(6)

$$Y = A + E \hspace{1cm} (6)$$

Elements in the matrix $A$ are the coefficients which can be found by least squares error method in equation (8):

$$A = (\Phi^T \Phi)^{-1} \Phi^T Y \hspace{1cm} (7)$$

In equation (8), $\Phi^T$ is the transpose of the matrix $\Phi$ and $(\Phi^T \Phi)^{-1}$ is the inverse of matrix. After obtaining the coefficients $a_1, a_2, ..., a_m$, the nodes location in the next time slot predicted using equation (3). If the node do not localized using WMCL algorithm with dynamic sampling, we will use this predicted location instead. Then the weights are computed for predicted samples.

D. Weighting the Samples

After a sample candidate is chosen, its weight is computed using 1-hop and 2-hop (anchor and common) neighbour nodes. Figure2 shows the phenomenon of weight computation.
In WMCL, $O_i \subseteq S \cup T \cup US$. So the weight of a candidate sample is computed as

$$w_i = p(O_i \mid l_i) = \prod_{s \in S \cup T \cup US} p(s \mid l_i) \prod_{s \in S \cup T \cup US} p(l_i \mid s)$$ (8)

When $s \in S$ or $s \in T$, $p(s \mid l_i)$ can be easily computed:

If $s \in S$, then

$$p(s \mid l_i) = [d(l_i, s) \leq r]$$ (9)

If $s \in T$, then

$$p(s \mid l_i) = [r < d(l_i, s) \leq 2r]$$ (10)

The weights of samples are computed. The samples with zero weights are rejected and samples with high weights are taken for error computation.

E. Error Computation

After obtaining $N$ valid samples, a sensor node computes the weighted average of these samples as its position estimation. Using the position estimation and the bounding-box, a sensor node can compute its $ER_x$ and $ER_y$, as illustrated in Figure 3.

A more risky method is to use the smallest rectangle enclosing all of $p$’s valid samples to compute $ER_x$ and $ER_y$. This method can improve localization accuracy a lot. However, when using this method the procedure of constructing the bounding-box should be carefully manipulated. In this case the inequality $p$ causes some inconsistency in the computation.
For example, it is possible that $x_{\text{min}}$ is larger than $x_{\text{max}}$ and consequently the bounding-box cannot be built. After $p$ gets $(x_e, y_e)$ and $E_{Rx}$, $E_{Ry}$, it broadcasts them to its neighbors. Its neighbors will use this information to compute their position estimation in the next time unit. Algorithm of the proposed method has been presented in figure (4).

```plaintext
if (ObservationSet, $\neq$ $\phi$) //The node see one or several anchor nodes
    $L_t = \phi$
    Compute $N$ // According to Equation6
    While (size ($L_t$) < $N$)
        Run WMCL Algorithm
        Location Estimation[i] = $\begin{bmatrix} y & 1 \\ x & 1 \end{bmatrix}$
    If trend line exist
        Update trend line in TSF
    else
        Return (-1)
else if (Number of Location Estimation[i] >= 4)
    Create trend line with Location Estimation[i]
    Calculate $<a_1, a_2, ..., a_m>$ $\leftarrow$ est_Coeficient()
    // estimate $a_1, a_2, ..., a_m$ based on the Modeling Window
    Calculate Location Estimation[i]
```

Figure 4: IMCL Algorithm

IV. RESULTS AND DISCUSSION

The simulation is carried out in NS-2 simulator under Linux platform with simulation area of 1000 x 1000m and 150 mobile nodes. The node is randomly placed from there onwards the node mobility occurs in random direction. The simulation time is 100 seconds.

A. Sampling efficiency

![Sampling efficiency graph](image)
The sampling efficiency is a very important metric in SMC-based localization algorithms because higher sampling means less candidate samples generation and consequently less computational cost. Figure (5) & (6) shows the number of candidate samples obtained for localization in the WMCL and IMCL algorithms with varying number of beacon and sensor nodes. The number of samples in WMCL algorithm is fixed and each unknown node during each time slot uses 50 samples to do localization. But in the IMCL algorithm samples number is determined dynamically. Simulation results show that with using IMCL algorithm, less candidate samples are chosen thereby obtaining high sampling efficiency. Each unknown node uses fewer samples than other methods.

B. Sampling Attempts

Most of computational energy consumption for these algorithms is related to the number of used samples and the number of sampling attempts to produce acceptable samples. Also the response time depends on the number of sampling attempts for production of required samples. Figure (6) shows simulation results for the number of sampling attempts to produce enough valid samples.

C. Dynamic Sampling

Figure 6: Samples Vs Sensor nodes

Figure 6: Sampling attempts

Figure 7: Dynamic sampling
The Dynamic sampling is performed in mobile nodes. Figure (7) shows the number of valid samples obtained for localization in the WMCL and IMCL algorithms. The number of samples in WMCL algorithm is fixed and each unknown node during each time slot uses 50 samples to do localization. But in the IMCL algorithm samples number is determined dynamically. Simulation results show that with using IMCL algorithm, each unknown node uses fewer samples than WMCL method.

D. Localization Accuracy

Localization accuracy is the most important metric in evaluating localization algorithms. The localization accuracy is determined from the estimated value of localization error. The localization error is noted for different time periods. The localization error is also determined by varying number of beacon and sensor nodes.

Figure (7) & (8) shows the localization error for varying number of beacon and sensor nodes. The graph shows that the localization error in IMCL algorithm is reduced compared with WMCL algorithm and thereby having high localization accuracy.

E. Energy backlog
The dynamic sampling method and TSF method used in IMCL algorithm will reduce the energy consumed in localization process by minimizing the number of sampling operation. Fig 10 shows the amount of energy consumed in IMCL algorithm is very much reduced than the WMCL algorithm.

V. CONCLUSION

The Improved Monte Carlo Localization (IMCL) algorithm achieved high sampling efficiency, high localization accuracy even in the case when there is a low beacon density using the bounding box and weight computation methods. The localization accuracy is improved by using the estimated position information of sensor nodes. The proposed IMCL algorithm used dynamic sampling based on the size of sampling area to estimate the sensor nodes position. Also the proposed algorithm uses TSF method to predict sensors position when the sensor nodes do not hear any anchor nodes. The proposed algorithm is suitable for mobile sensor networks with low anchor node density. This algorithm has less implementation costs in comparison with previous method. Simulation results showed that the proposed algorithm provides better performance than the similar method in the sparse sensor networks.

REFERENCES