# A hybrid approach to solve simultaneous scheduling problems in FMS 

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#### Abstract

Flexible Manufacturing System (FMS) executed number of advantages as far as decreasing cost, increased utilization of machine, condensed work-in-process levels, and so on. Notwithstanding, there are various issues faced during the life cycle of an FMS. In particular, the scheduling task, Scheduling of an FMS is a intricate problem to solve subsequently it has made enthusiasm among the scientists. Despite the fact that FMS scheduling problem was viewed before, scheduling of material handling system was not considered effectively. It is observed from the literature that for solving the simultaneous scheduling problems in FMS most of the researchers implemented Genetic algorithm (GA). In addition to Genetic Algorithm (GA) metaheuristics like Differential Evolution (DE), have been proved to be very effective in global optimization. In the current work a new hybrid metaheuristic (HDE) is proposed by amalgamating two metaheuristics namely Differential Evolution and Sheep Flock Heredity Algorithm (SFHA) for solving the simultaneous scheduling problems. The performance of the proposed algorithm HDE is assessed by solving 82 bench mark problems considered from the literature. The coding was done using java programing language.


Keywords - AGVs, FMS, Differential Evolution, Metaheuristic algorithms, Operational Completion Time (makespan), Sheep Flock Heredity Algorithm.

## I. INTRODUCTION

A Flexible Manufacturing System (FMS) is a profoundly automated manufacturing system appropriate for the concurrent creation of a wide assortment of part types in low to mid volume amounts at a low cost while keeping up a high caliber of the completed items. FMS executed number of advantages regarding decreasing cost - expanded use of machine-- condensed work-in - process levels and so forth. Anyway there are various issues faced during the life cycle of an FMS and these functions are characterized into: design- planning- scheduling- and controlling. Specifically the scheduling task and controlling issues during the manufacturing operation are of significance owing to the dynamic nature of the FMS in respect of flexible parts- tools- assignments. In FMS scheduling decisions that should be made incorporate not only sequencing of jobs on machines but also the routing of the jobs through the system. Apart from the machines different resources in the system like Automated Guided Vehicle (AGV) and Automated Storage/Retrieval System (AS/RS) must also taken in consideration. The AGVs effectiveness relies upon vehicle management system.

## II. LITERATURE REVIEW

Bilge and Ulusoy [1] addressed scheduling of machines and material handling system in an FMS simultaneously. A Sliding time window approach is used to solve the problem. The procedure is tested on 90 example problems. Abdelmaguid et al.[2] developed a new hybrid genetic algorithm/heuristic for solving simultaneous scheduling of machines and identical AGVs. The algorithm is implemented to a set of 82 bench mark problems considered from literature and the comparison of the results indicates the superior performance with the developed coding. Reddy and Rao [3] made an attempt to schedule machines and vehicles in FMS using evolutionary algorithms with minimization of makespan- mean flow
time and mean tardiness as an criterion. The proposed hybrid GA algorithm problems yielded better results when compared with other algorithms. Gnanavel babu et al. [4] proposed a new metaheuristic Differential Evolution algorithm for solving simultaneous scheduling of machines and two identical AGVs in FMS. Algorithm is tested on problems presented by various researchers and the obtained makespan is compared. Anandaraman et al. [5] addressed the scheduling of machines an AGV and two robots in a FMS with objectives to minimize the makespan, mean flow time and mean tardiness. The scheduling optimization is done using sheep flock heredity algorithm(SHFA) and Artificial immune system and the results obtained using the two algorithms are compared. Nouri et al. [6] proposed hybrid metaheuristic based on clustered Holonic Multiagent model. Computational results are presented using three sets of bench mark instances. Md Kamal et al. [7] presented a comprehensive literature review of the flexible job shop scheduling problem solved using GA. The survey is further extended by the inclusion of the hybrid GA techniques. Lundy et al.[8] proposes a model and proves that the algorithm converges with probability arbitrarily close to 1 . Finally described a version of the algorithm that terminates in polynomial time and allows a good deal of practical confidence in the solution. Storn [9] proposes a new heuristic approach for minimizing possibility non linear and non differentiable continous space functions. Which converges faster and with more certainity than both adaptive Simulated annealing and the Annealed Nelder \& Mead approach. Hyunchul [10] proposed anew evolutionary computation algorithm based on sheep flock heredity for solving large scale scheduling problem. This algorithm is able to find better solution than those of the simple genetic algorithm through thermal generator maintenance scheduling examples. Nageswara rao et al.[11] implemented three priority rules in solving simultaneous scheduling problems and the results are analyzed. Prakash babu et al.[12] implemented NEH heuristic to solve simultaneous scheduling problems in FMS. The heuristic is tested on 82 bench mark problems considered from literature. Prakash babu et al.[13] proposed new Fuzzy heuristic for solving simultaneous scheduling problem to minimize makespan. The algorithm is tested on 82 bench mark problems considered from literature. Prakash babu et al. [14] proposed a new hybrid metaheuristic JAYA (HJAYA) algorithm for solving simultaneous scheduling problems. The algorithm is implemented to 82 bench mark problems considered from the literature and results are compared. Prakash babu et al. [15] proposed a new hybrid metaheuristic hybrid Teaching Learning based optimization (HTLBO) algorithm for solving simultaneous scheduling problems. The algorithm is implemented to 82 bench mark problems considered from the literature and results are compared. Prakash babu et al. [16] implemented Differential evolution to solve simultaneous scheduling problems in FMS with minimization of makespan as criterion. It is tested on 82 bench mark problems considered from the literature and the results obtained are compared with the previously proposed algorithms.

## III. PROBLEM DESCRIPTION

Bilge and Ulusoy (1995) proposed a numerical example for simultaneous scheduling of machines and AGVs in FMS environment which incorporates four layouts- ten jobsets process times and travel time information as an input.

## IV. OBJECTIVE FUNCTION

The objective is to minimize the makespan, referred to as the maximum completion time of all the jobs Operation completion time $O_{i j}=T_{i j}+P_{i j}$
Where $\mathrm{T}_{\mathrm{ij}}$ and $\mathrm{P}_{\mathrm{ij}}$ are travel time, processing time for $j^{\text {th }}$ operation of the $i^{\text {th }}$ job, respectively.
Fob Completion time $C_{i}=\sum_{i=1}^{n} o_{i j}$
Makespan $=\operatorname{Max}\left(C_{1}, C_{2}, C_{3}, \ldots \ldots \ldots \ldots \ldots \ldots . . . . . . . . C_{n}\right)$
V. OPTIMIZATION PARAMETERS CONSIDERED

Population Size $=$ Double the no of operations
Iterations completed $=1000$

## VI. PROCEDURE FOR SIMULTANEOUS SCHEDULING OF MACHINES AND AGV,S

Jobs are scheduled based on the operation sequence derived by the algorithms. The problem considered needs scheduling of material handling system along with that of machines. The steps
implemented to obtain the makespan value for a given sequence of operations is indicated in the below flow chart.


Fig1: Simultaneous scheduling of machines and AGV,s

## VII. PROPOSED ALGORITHM

Since amalgamating of any two algorithms yields superior results, Differential Evolution is amalgamated with Sheep Flock Heredity Algorithm. Differential Evolution (DE) Algorithm was developed by Storn and Price (1995). The main working principle behind DE is the calculation of vector differences between randomly chosen population members. Sheep Flock Heredity Algorithm (SFHA) was developed by Hyunchul Kim (2001).This algorithm is based on the genetic inheritance. The cross over and mutation concepts hired from SFHA are incorporated into DE and the resulting algorithm is named as hybrid differential Evolution algorithm (HDE) in this work. The below flow chart indicates the steps involved in the proposed hybrid algorithm.


Fig:2 Flow chart for the proposed hybrid Differential Evolution (HDE) algorithm
For implementation of Hybrid Differential Evolution (HDE), Job set 7 and Layout 3 are considered as an example. HDE computes the vector differences between randomly chosen population members and receptor editing for different jobs and the sequences are obtained based on the mutation and crossover.

The HDE is explained in the following steps for the job set 7:
Step 1: Considering the job set

| Job set: 7 |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Layout: 3 |  |  | No of jobs: 8 |  |  | No of operations: 19 |  |  |
| Job 1 | Job 2 | Job 3 | Job 4 | Job 5 | Job 6 | Job 7 | Job 8 |  |
| M1-M4 | M2-M4 | M2-M4 | M3-M4 | M1-M3 | M2-M3-M4 | M1-M2-M3 | M1-M2-M4 |  |
| $1-2$ | $3-4$ | $5-6$ | $7-8$ | $9-10$ | $11-12-13$ | $14-15-16$ | $17-18-19$ |  |

In DE for the operation in a job set numbers are assigned serially.
Step 2: Generating the Population size (double the number of operations) randomly by using precedence relation i.e., operation of the same job set must be in increasing order but anywhere in the sequence. These are presented in Table. 1 and the steps shown in the Fig: 1 are implemented to identify the maximum operational completion time (makespan) for each sequence.

Table .1: Generated population size for the HDE

| S.No | Sequence | Makespan |
| :---: | :---: | :---: |
| 1 | 9-5-11-14-17-7-3-1-12-15-10-6-4-18-2-8-16-19-13 | 110 |
| 2 | 11-7-3-9-1-17-5-14-10-15-8-2-6-18-12-4-16-19-13 | 112 |
| 3 | 17-7-5-9-3-1-11-14-2-4-12-8-6-10-18-15-19-16-13 | 116 |
| 4 | 14-7-9-17-3-5-1-11-10-6-15-12-18-4-8-2-19-13-16 | 116 |
| 5 | 7-1-17-5-11-14-3-9-18-6-15-2-12-4-10-8-16-19-13 | 116 |
| 6 | 17-9-14-7-11-5-3-1-8-15-18-10-4-12-2-6-16-13-19 | 119 |
| 7 | 11-7-1-14-3-17-9-5-12-18-10-15-8-2-4-6-13-19-16 | 121 |
| 8 | 14-3-5-9-7-11-1-17-2-10-6-8-18-4-15-12-19-13-16 | 121 |
| 9 | 17-7-14-1-9-3-11-5-2-4-10-18-6-12-15-8-13-19-16 | 121 |
| 10 | 3-17-14-7-1-5-9-11-6-2-15-12-10-4-8-18-13-19-16 | 121 |
| 11 | 14-11-17-5-7-3-9-1-10-4-2-12-6-15-8-18-19-16-13 | 123 |
| 12 | 5-17-11-1-3-9-7-14-10-18-15-8-12-2-4-6-19-13-16 | 123 |
| 13 | 3-1-7-5-17-9-11-14-4-10-12-2-6-18-8-15-16-13-19 | 124 |
| 14 | 3-1-14-5-9-17-7-11-15-8-12-10-6-18-4-2-16-13-19 | 125 |
| 15 | 11-7-14-5-1-17-9-3-10-4-6-8-15-2-12-18-13-16-19 | 125 |
| 16 | 11-7-3-1-9-14-17-5-15-2-12-8-4-6-18-10-13-16-19 | 125 |
| 17 | 9-14-7-5-17-3-11-1-8-15-12-6-4-18-2-10-16-13-19 | 125 |
| 18 | 5-1-14-3-9-7-17-11-15-8-10-18-2-6-4-12-16-19-13 | 126 |
| 19 | 17-11-14-9-1-5-3-7-8-10-4-15-12-18-6-2-16-19-13 | 126 |
| 20 | 11-1-17-5-9-7-14-3-8-4-18-15-12-2-10-6-16-19-13 | 126 |
| 21 | 3-7-11-5-14-9-1-17-6-8-10-15-12-4-18-2-13-16-19 | 127 |
| 22 | 11-14-5-1-9-7-17-3-2-4-15-8-12-6-10-18-19-16-13 | 127 |
| 23 | 9-3-1-17-11-5-14-7-15-8-4-12-6-2-10-18-13-19-16 | 127 |
| 24 | 11-9-1-14-7-5-17-3-15-4-6-10-8-2-12-18-19-13-16 | 127 |
| 25 | 11-17-5-9-3-1-14-7-8-15-12-6-4-2-10-18-16-13-19 | 127 |
| 26 | 1-7-11-9-17-5-14-3-2-4-10-12-6-18-15-8-16-13-19 | 129 |
| 27 | 9-17-3-11-14-1-5-7-10-4-18-8-15-6-12-2-16-13-19 | 129 |
| 28 | 11-17-9-1-14-7-5-3-18-15-6-10-2-8-4-12-19-16-13 | 130 |
| 29 | 17-1-11-9-14-5-7-3-12-10-4-2-8-6-18-15-19-16-13 | 130 |
| 30 | 9-7-11-5-1-3-17-14-6-8-18-4-15-10-2-12-19-16-13 | 130 |
| 31 | 11-5-7-1-3-9-17-14-8-4-6-18-2-10-15-12-19-13-16 | 130 |
| 32 | 5-1-9-14-11-3-7-17-6-18-2-10-4-12-15-8-16-19-13 | 130 |
| 33 | 11-5-1-7-14-9-3-17-6-8-15-18-10-12-2-4-19-16-13 | 130 |
| 34 | 9-3-14-5-11-17-1-7-15-4-2-18-6-12-10-8-16-13-19 | 130 |
| 35 | 11-3-9-1-14-17-7-5-8-4-6-15-18-12-2-10-16-19-13 | 130 |
| 36 | 9-1-7-17-3-14-11-5-6-10-2-15-18-12-4-8-13-19-16 | 134 |
| 37 | 14-1-5-7-9-17-11-3-10-4-12-18-2-8-6-15-19-13-16 | 135 |
| 38 | 5-14-9-7-17-1-11-3-12-2-4-8-18-15-10-6-19-13-16 | 138 |

From the above Table it can be interpreted that in $1^{\text {st }}$ sequence, number ' 9 ' represents $1^{\text {st }}$ operation on the job no 5 and similarly number ' 5 ' represents the $1^{\text {st }}$ operation on job no 3 . Similarly number ' 19 ' represents 3 rd operation on job no 8 and so on.

Step 3: After all the sequences of the initial population have been evaluated, the best among them is taken. In this case the best among the initial population is
$X_{\text {best }}=9-5-11-14-17-7-3-1-12-15-10-6-4-18-2-8-16-19-13$--- 110
Step 4: Four vectors $X_{1}, X_{2}, X_{3} \& X_{4}$ will be randomly selected in the population is added to a best vector to get the resultant vector known as mutant vector
$\left(\mathrm{X}_{\text {new }}\right)$, as $\mathrm{X}_{\text {new }}=\mathrm{X}_{\text {best }}+\mathrm{F}_{1}\left(\mathrm{X}_{1}-\mathrm{X}_{2}\right)+\mathrm{F}_{2}\left(\mathrm{X}_{3}-\mathrm{X}_{4}\right)$ - (1)
9-5-11-14-17-7-3-1-12-15-10-6-4-18-2-8-16-19-13 $=X_{1}$
11-7-3-9-1-17-5-14-10-15-8-2-6-18-12-4-16-19-13 $=\mathrm{X}_{2}$
17-7-5-9-3-1-11-14-2-4-12-8-6-10-18-15-19-16-13 $=\mathrm{X}_{3}$
14-7-9-17-3-5-1-11-10-6-15-12-18-4-8-2-19-13-16 = $\mathrm{X}_{4}$
Subtracting and add these four vectors (absolute value is taken) and as suggested by Storn and Price [9] multiplying it with Factor $\mathrm{F}_{1}=0.65$ and $\mathrm{F}_{2}=0.85$ and rounding off, we get
$0.65\{(9-5-11-14-17-7-3-1-12-15-10-6-4-18-2-8-16-19-13)$ - (11-7-3-9-1-17-5-14-10-15-8-2-6-18-12-4-
$16-19-13)\}+0.85\{(17-7-5-9-3-1-11-14-2-4-12-8-6-10-18-15-19-16-13)-(14-7-9-17-3-5-1-11-10-6-15-12-$
18-4-8-2-19-13-16) \}
$=0.65(2-2-8-5-16-10-2-13-2-0-2-4-2-0-10-4-0-0-0)+0.85\{(3-0-4-8-0-4-10-3-8-2-3-4-12-6-10-13-0-3-3)$
$=(1-1-5-3-10-7-1-8-1-0-1-3-1-0-7-3-0-0-0)+(3-0-3-7-0-3-9-3-7-2-3-3-10-5-9-11-0-3-3)$
$=4-1-8-10-10-10-10-11-8-2-4-6-11-5-16-14-0-3-3$
Adding this with the best vector
9-5-11-14-17-7-3-1-12-15-10-6-4-18-2-8-16-19-13
We get
13-6-19-24-27-17-13-12-20-17-14-12-15-23-18-22-16-22-16
Now converting the values above 19 (max value allowed to values within bounds) we get
13-6-19-5-8-17-13-12-1-17-14-12-15-4-18-3-16-3-16
Step 5: Do the crossover operation for mutant vector
Mutant vector crossed over randomly with another population member
9-3-14-5-11-17-1-7-15-4-2-18-6-12-10-8-16-13-19
Chromosomes before crossover:
13-6-19-5- 8-17-13-12-1-17 +14-12-15- 4- 18- 3- 16- 3- 16
9-3-14-5-11-17-1-7-15-4 -2-18-6-12-10-8-16-13-19
Chromosomes crossover
13-6-19-5- 8-17-13-12-1-17-2-18-6-12-10- 8- 16-13-19
9-3-14-5-11-17-1-7-15-4-14-12-15-4-18- 3- 16- 3- $\mathbf{1 6}$
After crossover with crossover factor of 0.5 . we get the resulting vector as
13-6-19-5-8-17-13-12-1-17-2-18-6-12-10-8-16-13-19
Here it is observed that this vector doesn't contain all the operations and some operations are repeated. Hence the corrected repair function is used to avoid repetition and also used to include all the operations. So the resulting output after doing repair is
13-6-19-5-8-17-3-12-1-4-2-18-7-9-10-11-16-14-15
Repair function:
Repair function is used to make sure the vector so generated using random numbers follows precedence requirement constraints of the operations. If the precedence is not followed, the repair function swaps values within the array.
7-3-14-11-5-17-1-9-12-8-18-15-4-6-10-2-13-16-19
Step 5: After getting the final sequence from each iteration crossover and mutation concepts are implemented which are hired from sheep flock heredity algorithm.

Step 6: Receptor editing:
The process of removing the worst makespan value chromosomes from the population and replacing them with randomly generated chromosomes is called receptor editing. After this process a new population will be emerge this new population will become the input to the next iteration. This process continous until the termination criterion is reached.

Step 7: Termination criterion:
The above discussed procedure is repeated until the termination criteria is reached. In the present work repeating the procedure for more number of generations is considered as termination criterion.

Step 8: The best sequence and its related makespan obtained after completion of 1000 iterations is presented in Table .2.

Table.2: Operations schedule through HDE (for Problem set 7 and layout 3)

| Operation <br> Number | Machine <br> Number | Vehicle <br> Number | Travel <br> Time | Job <br> Reach | Job <br> Ready | Make <br> Span |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 5 | 2 | 1 | 0 | 4 | 4 | 13 |
| 7 | 3 | 2 | 0 | 10 | 10 | 26 |
| 3 | 2 | 1 | 28 | 32 | 32 | 43 |
| 14 | 1 | 1 | 14 | 16 | 16 | 26 |
| 6 | 4 | 1 | 18 | 26 | 26 | 33 |
| 11 | 2 | 2 | 14 | 18 | 18 | 31 |
| 4 | 4 | 1 | 4 | 12 | 12 | 21 |
| 9 | 1 | 2 | 28 | 30 | 30 | 39 |
| 12 | 3 | 1 | 32 | 38 | 38 | 57 |
| 17 | 1 | 1 | 42 | 44 | 44 | 55 |
| 10 | 3 | 2 | 39 | 47 | 57 | 75 |
| 1 | 1 | 2 | 51 | 53 | 55 | 61 |
| 2 | 4 | 1 | 44 | 54 | 54 | 60 |
| 15 | 2 | 2 | 53 | 55 | 55 | 64 |
| 18 | 2 | 1 | 58 | 60 | 64 | 73 |
| 8 | 4 | 2 | 61 | 63 | 63 | 70 |
| 13 | 4 | 1 | 66 | 68 | 70 | 76 |
| 16 | 3 | 2 | 69 | 75 | 75 | 88 |
| 19 | 4 | 1 | 74 | 82 | 82 | 90 |

Table 2 shows operation scheduling of through hybrid differential evolution algorithm for job set 7 layout 3 . From the table it is interpreted that operation 5 on machine 2 is completed by 13 min hence $3^{\text {rd }}$ operation will start after completion of $5^{\text {th }}$ operation on machine 2. In case of job set 7 and layout 3 operation 7 on machine 3 is completed by 26 min hence $12^{\text {th }}$ operation on machine 3 will start after completion of $7^{\text {th }}$ operation on machine 2 . Similarly, no operation on the particular machine will start until the operation on the machine is completed. From the vehicle heuristic algorithm for first two operations AGVs are selected randomly in case of third operation AGV ' 1 ' is selected basing on the availability of AGV with minimum travel time this constraint will be taking care in the algorithm, for job set 7 and layout 3 the operational completion time (makespan) is 90 .

## VIII. RESULTS AND DISCUSSION

Computations for makespans for different combinations of job sets and layouts for hybrid differential evolution algorithm, Priority rules (FCFS, SPT, LPT, Nageswararao et al. 2017), Heuristic (NEH, Prakash babu et al, 2018, FUZZY, P. B. Kanakavalli et al, 2018) with $t / p>0.25$ are presented in Table 3. A code is used to designate the example problems which are given in the first column. The digits that follow 1.1 indicate the job set and the layout. In $\mathrm{t} / \mathrm{p}$ ratio $<0.25$ table another digit is appended to the code. Herehaving a 0 or 1 as the last digit implies that the process times are doubled or tripled- respectively- where in both cases travel times are halved.

Table .3: Comparison of make span values (for $\mathrm{t} / \mathrm{p}>0.25$ )

| Job. No | t/p | FCFS | SPT | LPT | NEH | FUZZY | HDE |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.1 | 0.59 | 173 | 193 | 177 | 165 | 208 | 96 |
| 2.1 | 0.61 | 158 | 158 | 177 | 169 | 170 | 98 |
| 3.1 | 0.59 | 202 | 224 | 198 | 195 | 211 | 109 |
| 4.1 | 0.91 | 263 | 267 | 264 | 260 | 268 | 116 |
| 5.1 | 0.85 | 148 | 164 | 148 | 147 | 174 | 89 |
| 6.1 | 0.78 | 231 | 240 | 227 | 225 | 233 | 113 |
| 7.1 | 0.78 | 195 | 210 | 201 | 173 | 196 | 121 |
| 8.1 | 0.58 | 261 | 261 | 266 | 261 | 261 | 150 |
| 9.1 | 0.61 | 270 | 277 | 268 | 259 | 273 | 116 |
| 10.1 | 0.55 | 308 | 308 | 310 | 305 | 315 | 167 |
| 1.2 | 0.47 | 143 | 173 | 165 | 147 | 188 | 82 |
| 2.2 | 0.49 | 124 | 124 | 130 | 116 | 127 | 76 |
| 3.2 | 0.47 | 162 | 188 | 160 | 154 | 178 | 83 |
| 4.2 | 0.73 | 217 | 223 | 224 | 215 | 232 | 90 |
| 5.2 | 0.68 | 118 | 144 | 131 | 117 | 156 | 73 |
| 6.2 | 0.54 | 180 | 169 | 165 | 158 | 175 | 90 |
| 7.2 | 0.62 | 149 | 160 | 149 | 136 | 139 | 85 |
| 8.2 | 0.46 | 181 | 181 | 198 | 181 | 181 | 131 |
| 9.2 | 0.49 | 250 | 249 | 244 | 205 | 249 | 104 |
| 10.2 | 0.44 | 290 | 288 | 287 | 274 | 274 | 149 |
| 1.3 | 0.52 | 145 | 175 | 167 | 145 | 190 | 84 |
| 2.3 | 0.54 | 130 | 130 | 136 | 122 | 133 | 82 |
| 3.3 | 0.51 | 160 | 190 | 162 | 158 | 176 | 86 |
| 4.3 | 0.8 | 233 | 237 | 230 | 226 | 234 | 96 |
| 5.3 | 0.74 | 120 | 146 | 133 | 117 | 156 | 76 |
| 6.3 | 0.54 | 182 | 171 | 167 | 160 | 177 | 92 |
| 7.3 | 0.68 | 155 | 166 | 151 | 138 | 141 | 90 |
| 8.3 | 0.5 | 183 | 183 | 200 | 183 | 183 | 133 |
| 9.3 | 0.53 | 252 | 251 | 246 | 207 | 251 | 105 |
| 10.3 | 0.49 | 293 | 294 | 293 | 280 | 280 | 129 |
| 1.4 | 0.74 | 189 | 207 | 189 | 189 | 228 | 104 |
| 2.4 | 0.77 | 174 | 174 | 174 | 169 | 190 | 112 |
| 3.4 | 0.74 | 220 | 250 | 212 | 213 | 225 | 113 |
| 4.4 | 1.14 | 301 | 301 | 298 | 298 | 294 | 128 |
| 5.4 | 1.06 | 171 | 189 | 171 | 171 | 193 | 97 |
| 6.4 | 0.78 | 249 | 252 | 237 | 234 | 243 | 119 |
| 7.4 | 0.97 | 217 | 242 | 151 | 192 | 232 | 135 |
| 8.4 | 0.72 | 285 | 285 | 200 | 285 | 285 | 152 |
| 9.4 | 0.76 | 292 | 311 | 290 | 285 | 295 | 125 |
| 10.4 | 0.69 | 350 | 350 | 345 | 345 | 353 | 161 |

The optimal sequence of machines and AGVs are determined by using FCFS-SPT- LPT-NEHFUZZY and HDE for $t / p>0.25$ are shown in Table.3. From Table 3 it can be observed that, out of 40 problems, 40 problems give better results using HDE when compared with all other five algorithms .Computations for completion time for different combinations of job sets and layouts for four metaheuristic and one hybrid metaheuristic algorithms with $\mathrm{t} / \mathrm{p}<0.25$ are done and tabulated in Table 4.

Table 4.Comparison of make span values (for $\mathrm{t} / \mathrm{p}<0.25$ )

| Job.No | $\mathrm{t} / \mathrm{p}$ | FCFS | SPT | LPT | NEH | FUZZY | HDE |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.10 | 0.15 | 207 | 248 | 252 | 207 | 278 | 126 |
| 2.10 | 0.15 | 217 | 217 | 225 | 185 | 208 | 131 |
| 3.10 | 0.15 | 257 | 327 | 282 | 255 | 300 | 143 |
| 4.10 | 0.15 | 303 | 328 | 317 | 277 | 352 | 123 |
| 5.10 | 0.21 | 152 | 190 | 187 | 154 | 225 | 102 |
| 6.10 | 0.16 | 304 | 281 | 297 | 272 | 294 | 146 |
| 7.10 | 0.19 | 231 | 240 | 264 | 213 | 235 | 137 |
| 8.10 | 0.14 | 338 | 338 | 347 | 332 | 338 | 247 |
| 9.10 | 0.15 | 390 | 367 | 359 | 324 | 382 | 182 |
| 10.10 | 0.14 | 452 | 429 | 444 | 398 | 393 | 218 |
| 1.20 | 0.12 | 194 | 238 | 246 | 197 | 268 | 123 |
| 2.20 | 0.12 | 194 | 194 | 206 | 167 | 187 | 128 |
| 3.20 | 0.12 | 241 | 311 | 270 | 241 | 285 | 139 |
| 4.20 | 0.12 | 285 | 312 | 298 | 248 | 340 | 116 |
| 5.20 | 0.17 | 142 | 180 | 184 | 143 | 217 | 100 |
| 6.20 | 0.12 | 292 | 260 | 284 | 251 | 277 | 141 |
| 7.20 | 0.15 | 212 | 218 | 249 | 188 | 210 | 136 |
| 8.20 | 0.11 | 306 | 319 | 334 | 306 | 306 | 244 |
| 9.20 | 0.12 | 380 | 355 | 347 | 309 | 372 | 179 |
| 10.20 | 0.11 | 445 | 423 | 439 | 388 | 384 | 212 |
| 1.30 | 0.13 | 195 | 239 | 247 | 196 | 169 | 122 |
| 2.30 | 0.13 | 197 | 197 | 209 | 170 | 190 | 129 |
| 3.30 | 0.13 | 240 | 312 | 271 | 240 | 284 | 138 |
| 4.30 | 0.13 | 292 | 317 | 301 | 255 | 339 | 117 |
| 5.30 | 0.18 | 141 | 181 | 183 | 143 | 216 | 99 |
| 6.30 | 0.24 | 296 | 261 | 285 | 252 | 278 | 141 |
| 7.30 | 0.17 | 215 | 221 | 250 | 191 | 213 | 137 |
| 8.30 | 0.13 | 307 | 320 | 335 | 307 | 307 | 245 |
| 9.30 | 0.13 | 381 | 356 | 348 | 310 | 373 | 180 |
| 10.30 | 0.12 | 448 | 426 | 442 | 391 | 387 | 191 |
| 1.40 | 0.18 | 213 | 255 | 254 | 213 | 288 | 124 |
| 2.41 | 0.13 | 307 | 307 | 319 | 267 | 293 | 191 |
| 3.40 | 0.18 | 261 | 330 | 282 | 258 | 305 | 143 |
| 3.41 | 0.12 | 370 | 476 | 411 | 310 | 435 | 209 |
| 4.41 | 0.19 | 434 | 471 | 451 | 393 | 504 | 177 |
| 5.41 | 0.18 | 218 | 269 | 270 | 222 | 321 | 148 |
| 6.40 | 0.19 | 310 | 288 | 299 | 275 | 303 | 151 |
| 7.40 | 0.24 | 239 | 251 | 270 | 221 | 246 | 137 |
| 7.41 | 0.16 | 329 | 344 | 385 | 224 | 332 | 203 |
| 8.40 | 0.18 | 343 | 343 | 349 | 339 | 343 | 248 |
| 9.40 | 0.19 | 396 | 379 | 370 | 325 | 388 | 182 |
| 10.40 | 0.17 | 466 | 445 | 455 | 415 | 408 | 214 |

The optimal sequence of machines and AGVs are determined by using FCFS-SPT- LPT- NEH-FUZZY and HDE for $\mathrm{t} / \mathrm{p}<0.25$ are shown in Table 4. From Table 4 it can be observed that out of 42 problems, 42 problems give better results using HDE when compared with all other five algorithms.

## IX. CONCLUSION

Flexible Manufacturing system is considered as better choice to confront the difficulties of global competition. But for successful implementation efficient scheduling is essential. Scheduling of an FMS is a very difficult problem because of other consideration like material handling. In this work an endeavor
has been made to tackle the problem of scheduling both the machines and AGVs simultaneously by a hybrid metaheuristic algorithm. The following conclusions are drawn from this work. Execution of the proposed Hybrid Metaheuristic Algorithm is assessed by considering 82 benchmark problems comprising of various jobsets and layout configurations. From the results it is observed that the proposed hybrid Differential Evolution (HDE) algorithm yielded improved results in all the 82 problems when compared with the other algorithms.

## X. SCOPE OF FUTURE WORK

In the present work a hybrid metaheuristic is proposed to solve simultaneous scheduling of problems in FMS. There is scope for further research work in the following aspects: In FMS jobs enter with different priorities and the problem can be made dynamic in nature. When required sequence needs to reschedule. The simultaneous scheduling problem can be extended further by including AS/RS system. Real time issues like traffic jamming- without buffer space and machine breakdowns can also be considered.

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